

# Sierpinski Triangles

A Sierpinski triangle is a fractal shape. Fractal math occurs in nature and you can spend hours exploring interesting patterns on the internet and trying to find them in nature. Fractals are never-ending repeating patterns. Of course, we don't have an infinite amount of time available to draw never-ending images so we'll show you how to draw a Stage 3 Sierpinski triangle.

Here's what we'll be constructing.....

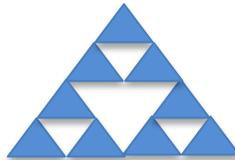
**Stage 0 Triangle**



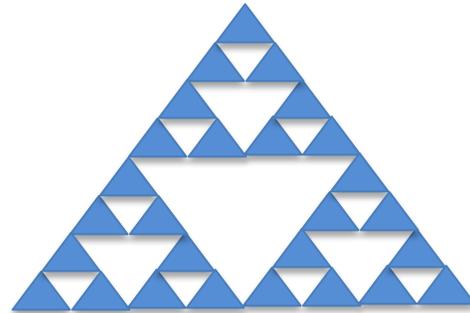
**Stage 1 Triangle**



**Stage 2 Triangle**



**Stage 3 Triangle**



## Instructions for Drawing a Stage 3 Sierpinski Triangle

Step 1: Use the triangle template on the next page along with a ruler and a pencil

Step 2: Measure each side of the triangle and make a mark at the midpoint of each side (We've made a mark for the midpoint of the bottom side on the template).

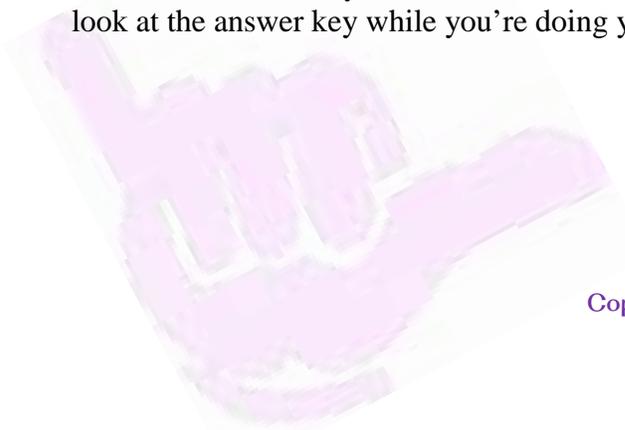
Step 3: Once you've marked the midpoint of each side, use your ruler to draw a line connecting each midpoint. When you have completed this, you'll have the framework for the Stage 1 Triangle you see above (we won't be shading in the upright triangles until the end).

Step 4: Now, use your Stage 1 triangle to construct a Stage 2 triangle. For each upright triangle (point on the top and base on the bottom), repeat steps 2 and 3. This will give you a Stage 2 triangle.

Step 5: Again, use your Stage 2 triangle to construct a Stage 3 triangle by repeating steps 2 and 3 for each upright triangle you have.

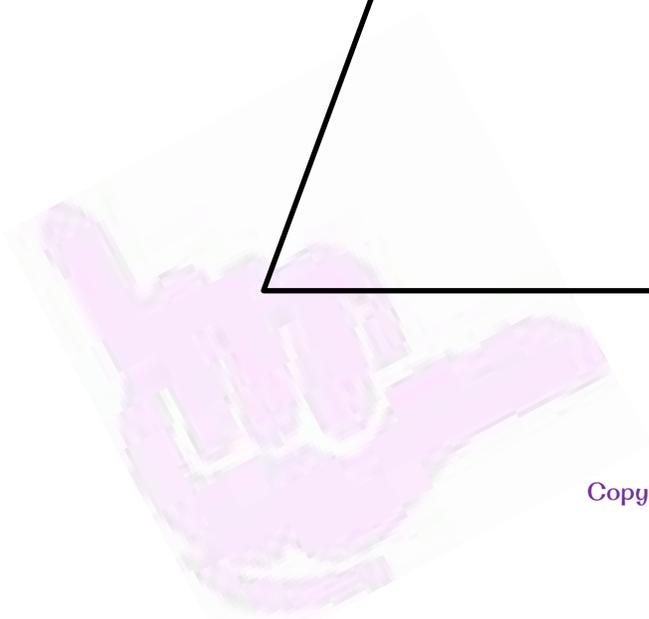
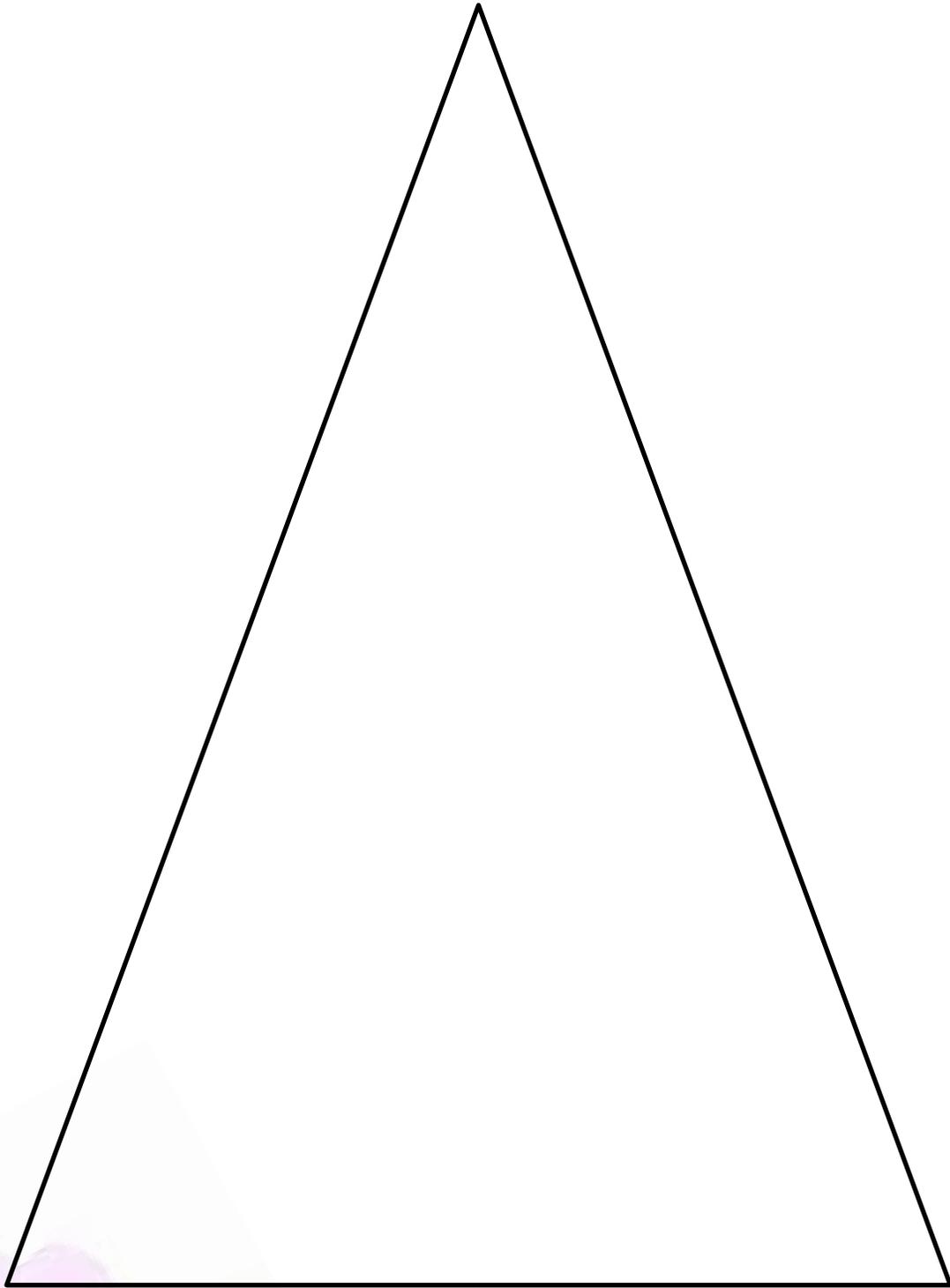
Step 6: Now that you have the framework for the Stage 3 triangle, you can color in the upright triangles to match what is shown above.

Note: The answer key shows the framework for all stages. This is one case where it's perfectly acceptable to look at the answer key while you're doing your work!



# Sierpinski Triangles

Triangle Template



# Sierpinski Triangles

## CHALLENGE QUESTIONS

Test your knowledge of Sierpinski triangles by answering these challenge questions.

1. How many shaded triangles are in a Stage 0 Sierpinski triangle? Stage 1? Stage 2? Stage 3?
2. What about a Stage 4 Sierpinski triangle? How many shaded triangles would be in this stage?
3. What would be the general rule that predicts the number of shaded triangles for a given stage? For example, could you write the expression for the number of shaded triangles in a Stage 50 Sierpinski triangle?
4. At what stage do we have 243 shaded triangles?
5. What is the ratio of base length to altitude height for a Stage 0 triangle? What about the ratio of base length to altitude height for a shaded triangle in a Stage 1 Sierpinski figure?
6. Search for fractal shapes on the internet. What's your favorite shape?
7. Once you've practiced precisely drawing Sierpinski triangles, check out Vi Hart's video (<https://www.youtube.com/watch?v=EdyociU35u8>). You'll see how to draw other fractal patterns such as dragon curves and see how they can be related to Sierpinski triangle structures.



# Sierpinski Triangles

## CHALLENGE QUESTIONS

Test your knowledge of Sierpinski triangles by answering these challenge questions.

1. How many shaded triangles are in a Stage 0 Sierpinski triangle? Stage 1? Stage 2? Stage 3?  
STAGE 0 = 1 TRIANGLE; STAGE 1 = 3 TRIANGLES; STAGE 2 = 9 TRIANGLES; STAGE 3 = 27 TRIANGLES

2. What about a Stage 4 Sierpinski triangle? How many shaded triangles would be in this stage?  
STAGE 4 = 81 TRIANGLES

3. What would be the general rule that predicts the number of shaded triangles for a given stage? For example, could you write the expression for the number of shaded triangles in a Stage 50 Sierpinski triangle?

SHADED TRIANGLES FOR STAGE  $N = 3^N$

4. At what stage do we have 243 shaded triangles?

$243 = 3^N \rightarrow N = 5$  WE HAVE A STAGE 5 TRIANGLE

5. What is the ratio of base length to altitude height for a Stage 0 triangle? What about the ratio of base length to altitude height for a shaded triangle in a Stage 1 Sierpinski figure?

STAGE 0 BASE TO HEIGHT RATIO: 14 TO 19

STAGE 1 BASE TO HEIGHT RATIO FOR SHADED TRIANGLE: 14 TO 19

6. Search for fractal shapes on the internet. What's your favorite shape?

SOME OF OUR FAVORITE SHAPES ARE SIERPINSKI TRIANGLES, DRAGON CURVES, MANDELBROT SET AND MENGER SPONGE – MAYBE YOU'LL CREATE A NEW SHAPE THAT WILL BECOME ONE OF OUR NEW FAVORITES!

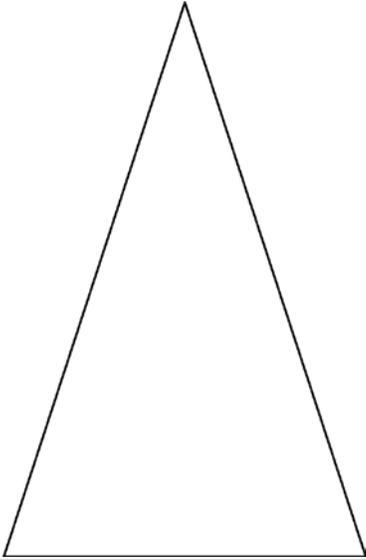
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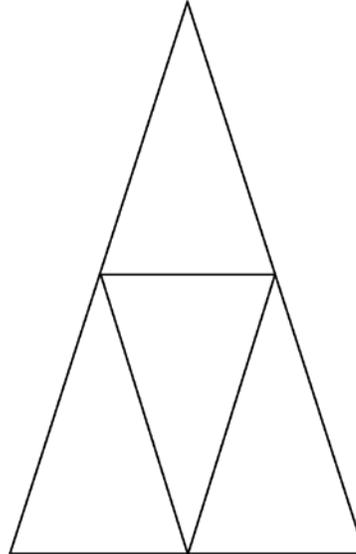
# Sierpinski Triangles

## SIERPINSKI TRIANGLE FRAMEWORKS

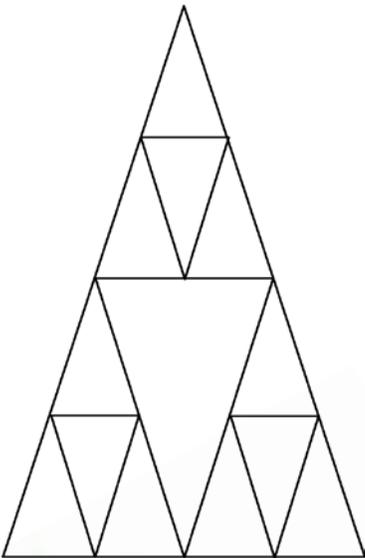
STAGE 0 TRIANGLE



STAGE 1 TRIANGLE



STAGE 2 TRIANGLE



STAGE 3 TRIANGLE

